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## 誌謝

需要感謝的人太多了，就感謝天罷！  
你的論文趕快寫完，就謝天謝地嘍！

## Abstract

Content of abstract

**Keywords:** *Cryptography*

# 摘要

摘要內容

關鍵字: 臺大椰林、總圖。

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# Chapter 1

## Introduction

This is an example of table. We recommend the online Latex Generator: <https://www.tablesgenerator.com/>

Algorithm	Time Complexity	Space Complexity
AKS Sieve [AKS01]	$2^{3.346n+o(n)}$	$2^{2.173n+o(n)}$

Table 1.1: Example of table

### 1.1 Contributions and Roadmap

write it down or not.

- **Taiwan No. 1 Good**



Figure 1.1: Just an example

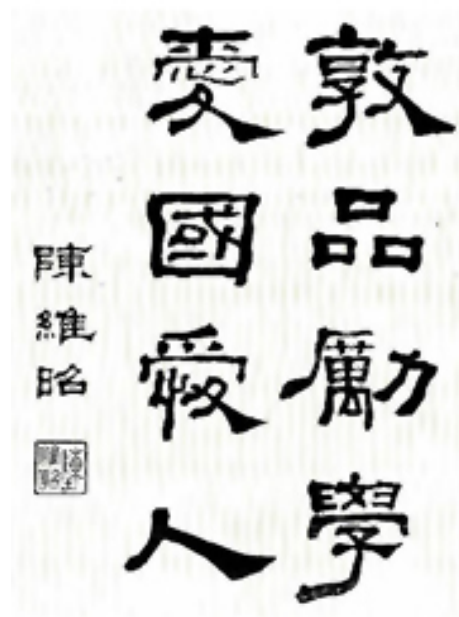


Figure 1.2: me too

# Chapter 2

## Preliminary

### 2.1 Definition and Notation

This is different

Examples

Problem Descriptions

**Problem Property** This is an example of equations.

$$\left\| \sum_{t=1}^n u_t \vec{b}_t \right\| = \min_{x \in \mathbb{Z}^n} \left\| \sum_{t=1}^n x_t \vec{b}_t \right\|$$

we replace all  $\vec{b}_t$  by their orthogonalization, i.e.,  $\vec{b}_t = \vec{b}_t^* + \sum_{j=1}^{t-1} \mu_{t,j} \vec{b}_j^*$  and get a degree.

---

**Algorithm 1** This is an example of algorithm.

---

**Require:** basis  $B(\vec{b}_1, \dots, \vec{b}_n)$ , PrunedBound  $R_1^2 \leq R_2^2 \leq \dots \leq R_n^2$

**Ensure:** The coefficients  $(x_1, \dots, x_n)$  of the basis satisfying the Pruned Bound

Compute Gram-Schmidt orthogonalization  $\mu$  of basis  $B$

$\sigma \leftarrow (0)_{(n+1) \times n}$

**while true do**

$\rho_k = \rho_{k+1} + (v_k - c_k)^2 \|\vec{b}_k^*\|^2$

**if**  $\rho_k \leq R_{n+i-k}^2$  **then**

**if**  $k = 1$  **then**

return  $(v_1, \dots, v_n)$

**else**

$k \leftarrow k - 1$

$r_{k-1} \leftarrow \max(r_{k-1}, r_k)$

**for**  $i = r_k$  **downto**  $k + 1$  **do**

$\sigma_{i,k} \leftarrow \sigma_{i+1,k} + v_k \mu_{i,k}$

**end for**

$c_k \leftarrow -\sigma_{k+1,k}$

$v_k \leftarrow \lfloor c_k \rfloor$ ;  $w_k = 1$ ;

**end if**

**else**

$k \leftarrow k + 1$

**end if**

**end while**

---

# Bibliography

- [AKS01] Miklós Ajtai, Ravi Kumar, and D. Sivakumar. A sieve algorithm for the shortest lattice vector problem. In Jeffrey Scott Vitter, Paul G. Spirakis, and Mihalis Yannakakis, editors, *Proceedings on 33rd Annual ACM Symposium on Theory of Computing, July 6-8, 2001, Heraklion, Crete, Greece*, pages 601–610. ACM, 2001.

# Appendices

# Appendix A

## Proof for example

### A.1 title

Here we consider the case of  $q = 12289$ ,  $k = 3$ . The input  $U, V$  satisfies the following condition.

$$V = V_0 + V_1 \cdot 2^{12} + V_2 \cdot 2^{24} \text{ and } U = U_0 + U_1 \cdot 2^{12}$$

where  $0 \leq V_0 < 2^{12}$ ,  $0 \leq V_1 < 2^{12}$ ,  $0 \leq V_2 < 2^6$ ,  $0 \leq U_0 < 2^{12}$ , and  $0 \leq U_1 < 2^4$

$$A = \text{K-RED}(U) = 3U_0 - U_1 \text{ and } B = \text{K-RED2x}(V) = 9V_0 - 3V_1 + V_2$$